## Series \& Parallel Circuits

|  | CONNECTED IN SERIES | CONNECTED IN PARALLEL |
| ---: | :---: | :---: |
| Voltage | $\mathrm{V}_{\mathrm{T}}=\mathrm{V}_{1}+\mathrm{V}_{2}+\mathrm{V}_{3}+\cdots$ | $\mathrm{V}_{\mathrm{T}}=\mathrm{V}_{1}=\mathrm{V}_{2}=\mathrm{V}_{3}=\cdots$ |
| Current | $\mathrm{I}_{\mathrm{T}}=\mathrm{I}_{1}=\mathrm{I}_{2}=\mathrm{I}_{3}=\cdots$ | $\mathrm{I}_{\mathrm{T}}=\mathrm{I}_{1}+\mathrm{I}_{2}+\mathrm{I}_{3}+\cdots$ |
| Resistance | $\mathrm{R}_{\mathrm{T}}=\mathrm{R}_{1}+\mathrm{R}_{2}+\mathrm{R}_{3}+\cdots$ | $\frac{1}{\mathrm{R}_{\mathrm{T}}}=\frac{1}{\mathrm{R}_{1}}+\frac{1}{\mathrm{R}_{2}}+\frac{1}{\mathrm{R}_{3}}+\cdots$ |
| Power | $\mathrm{P}_{\mathrm{T}}=\mathrm{P}_{1}+\mathrm{P}_{2}+\mathrm{P}_{3}+\cdots$ | $\mathrm{P}_{\mathrm{T}}=\mathrm{P}_{1}+\mathrm{P}_{2}+\mathrm{P}_{3}+\cdots$ |

Ohm's Law: $V=I R \quad$ power: $P=V I=I^{2} R=\frac{V^{2}}{R}$
$n$ identical resistors in series: $\quad R_{T}=n R$
$n$ identical resistors in parallel: $\quad R_{T}=\frac{R}{n}$
short cut for 2 resistors in parallel: $\quad R_{T}=\frac{R_{1} R_{2}}{R_{1}+R_{2}}$

## EXERCISES

A. Considering the following circuit, complete the table:


|  | $\mathbf{R}_{\mathbf{1}}$ | $\mathbf{R 2}_{\mathbf{2}}$ | $\mathbf{R}_{\mathbf{3}}$ | $\mathbf{R}_{\text {total }}$ |
| ---: | :---: | :---: | :---: | :---: |
| Voltage (V) |  |  |  | 12 |
| Current (A) |  |  |  |  |
| Resistance ( $\Omega$ ) | 150 | 220 | 470 |  |
| Power (W) |  |  |  |  |

B. Considering the following circuit, complete the table:


|  | $\mathbf{R 1}_{\mathbf{1}}$ | $\mathbf{R 2}_{\mathbf{2}}$ | $\mathbf{R}_{\mathbf{3}}$ | $\mathbf{R T O T A L}$ |
| ---: | :---: | :---: | :---: | :---: |
| Voltage (V) |  |  |  | 15 |
| Current (A) |  |  |  |  |
| Resistance ( $\Omega$ ) | 120 | 180 | 270 |  |
| Power (W) |  |  |  |  |

C. Considering the following circuit, complete the table:


|  | $\mathbf{R 1}_{1}$ | $\mathbf{R 2}_{2}$ | $\mathbf{R 3}_{3}$ | $\mathbf{R}_{\mathbf{4}}$ | Rtotal |
| ---: | :---: | :---: | :---: | :---: | :---: |
| Voltage (V) |  |  |  |  | 10 |
| Current (A) |  |  |  |  |  |
| Resistance ( $\Omega$ ) | 56 | 27 | 47 | 15 |  |
| Power (W) |  |  |  |  |  |

D. Twenty resistors, each with a resistance of $22 \Omega$, are connected in series. What is the total resistance?
E. Ten resistors, each with a resistance of $1000 \Omega$, are connected in parallel. What is the total resistance?
F. Three resistors can be connected in a variety of ways to obtain eight different resistances. What resistances can be obtained with each of the following? [Hint: First, figure out what four configurations there can be with three resistors.]

1) $18 \Omega, 56 \Omega, 82 \Omega$
2) $220 . \Omega, 330 . \Omega, 470 . \Omega$

## SOLUTIONS

A.

|  | $\mathbf{R}_{\mathbf{1}}$ | $\mathbf{R}_{\mathbf{2}}$ | $\mathbf{R}_{\mathbf{3}}$ | $\mathbf{R}_{\mathbf{T}}$ |
| ---: | :---: | :---: | :---: | :---: |
| $\mathbf{V}$ | 2.1 | 3.1 | 6.7 | $\mathbf{1 2}$ |
| $\mathbf{I}$ | .014 | .014 | .014 | .014 |
| $\mathbf{R}$ | $\mathbf{1 5 0}$ | $\mathbf{2 2 0}$ | $\mathbf{4 7 0}$ | 840 |
| $\mathbf{P}$ | .031 | .045 | .096 | .171 |
| D. | $440 \Omega$ | $\mathrm{E} .100 \Omega$ |  |  |


| B. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | R1 | R2 | R3 | RT |
| V | 15 | 15 | 15 | 15 |
| I | 0.13 | . 083 | . 056 | 0.26 |
| R | 120 | 180 | 270 | 56.8 |
| P | 1.9 | 1.3 | 0.83 | 4.0 |


| C. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | R1 | R2 | R3 | R4 | RT |
| V | 4.5 | 2.2 | 6.7 | 3.3 | 10 |
| I | . 080 | . 080 | 0.14 | 0.22 | 0.22 |
| R | 56 | 27 | 47 | 15 | 45 |
| P | 0.36 | 0.17 | 0.95 | 0.74 | 2.2 |

F. (1) $12 \Omega, 16 \Omega, 36 \Omega, 39 \Omega, 51 \Omega, 71 \Omega, 96 \Omega, 156 \Omega$
(2) $103 \Omega, 173 \Omega, 223 \Omega, 253 \Omega, 414 \Omega, 480 \Omega, 602 \Omega, 1020 \Omega$

